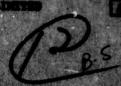


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UNGUIDED MOCKET DEACT DISPERSION AT WELLE SANDS MISSILE RANGE, NEW MEXICO

DAYED J. MOVLAN



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UNITED STATES ARMY ELECTRONICS COMMAND

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DR-937			
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WHITE SANDS MISSILE RANGE, NEW ME		6. PERFORMING ORG. REPORT NUMBER	
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PERFORMING ORGANIZATION NAME AND ADDRESS		10. PROGRAM ELEMENT, PROJECT, TAS AREA & WORK UNIT NUMBERS	
Meteorological data repty		(12) 42	
CONTROLLING OFFICE NAME AND ADDRESS		12. REPORT DATE	
US Army Electronics Command		February 1977	
Atmospheric Sciences Laboratory	wise.	13. NUMBER OF PAGES	
White Sands Missile Range, New Me MONITORING AGENCY NAME & ADDRESS(II differen	nt from Controlling Office)	15. SECURITY CLASS. (of this report)	
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20. ABSTRACT (Cont) TO PIGE 34

sophisicated impact prediction and measurement techniques utilized during this period. A scatter diagram is presented for each rocket showing the area of primary dispersion of each shot around the predicted impact point. Included on each diagram is the standard error of estimate (total and component form) for each rocket type and the number of cases on which the calculations were based. All cases involving a known rocket malfunction were excluded from this study. In addition, theory on the deviations of "box limits" (T-90 second tower constraints) is presented, and actual recommended limits for each type of rocket are computed.

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FOREWORD

This report is a revision of Data Report 821, "Unguided Rocket Impact Dispersion at White Sands Missile Range, New Mexico," published in March 1974. This revision summarizes the dispersion of many unguided missiles fired at White Sands Missile Range and the Utah Launch Complex at Green River, Utah, from 1970 to 1976.



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INTRODUCTION

The statistical scatter of the actual impact points about the predicted impact point of an unguided rocket is the rocket's impact dispersion.

The causes of rocket impact dispersion can be divided into five basic categories: 1) variations in atmospheric components, 2) variations in rocket components, 3) rocket misalignments, 4) launcher misalignments, and 5) factors which do not vary but are not precisely evaluated or are unaccounted for.

Before an unguided rocket is flight-tested, a theoretical dispersion study is usually performed to estimate its dispersion. This analysis can be made using a trajectory simulation program in a high-speed computer. The best estimates available of the perturbing factors can be put in the program, and the impact points can be compared with the nominal impact point. When this procedure is used, it is assumed that the perturbing factors act independently.

The six-year period from 1970-1976 was chosen for this study because of the more advanced and sophisicated impact prediction and measurement techniques used during this period; namely, T-9 radar pibal tracking, advanced Wang calculators utilized on hot firings, impact predictions using 5-D real-time systems (2), HP-97 field backups, etc.

Dispersion for each rocket firing is plotted on a Cartesian coordinate scatter diagram showing the misses around the predicted impact (origin of the coordinate system). The dispersion for each type of rocket is then analyzed in terms of the standard error of estimate (both total and in component form). All cases that involved a known rocket malfunction were not included in this study.

This report presents the actual impact dispersion of twenty-four unguided rockets fired at White Sands Missile Range (WSMR), New Mexico, or the Utah Launch Complex, Green River, Utah, for the period 1970-1976. No attempt is made to isolate the various causes of dispersion.

The actual impact points were taken from surveys when available. Elsewhere, radar or Sonic Observation of Trajectory and Impact of Missiles (SOTIM) impact data were used.

This information should be helpful for range planning and safety considerations.

Figure 1 shows the White Sands Missile Range (regular Range) along with its extended borders.

For major unguided rocket launches (excluding small meteorological rockets fired from Small Missile Range), one of the major factors influencing the impact predictor's decision to recommend fire, delay or hold is the constraint put on the 500 foot winds. This constraint is referred to as the "box limits." For most unguided rocket firings, nearly 50% of the wind weighting has occurred in the lowest 500 feet of its trajectory after lift-off with nearly 75-85% of the total correction experienced by the time the rocket has flown some 4000 feet after lift-off. These box limits are computed around T-90 to T-60 seconds, and the weighted 500 foot average wind is allowed to wander inside these limits up to T-0 to assure a safe firing. If the variability of the wind is such that the weighted 500 foot wind during this crucial part of the count-down wanders outside these limits, then a delay count or a hold is initiated. The actual positioning of these limits is determined by the total displacement in the 500 foot wind at finals time* and the change in the weighted winds from 4500-8000 feet mean sea level from the latest two balloon runs.

It is recommended that the actual size of these box limits be determined by the following method or at least have this procedure serve as guidance. Using the statistics compiled in this report (namely the components of the standard error of estimate), the missile range (regular boundaries) will be reduced as follows (see Figure 2):

- 1. Utilize a 40 mile wide, 65 mile long missile range (that is the range north of the WSNM).
- 2. Use the center of this rectangular range as impact point.
- 3. As in Figure 2 reduce the east-west boundaries by coming in $2S_X$ from each boundary (where S_X has been defined previously) and analogously for reducing the north-south boundaries. This will produce box limits of \pm 1 for the east-west and \pm 2 for the north-south where:

$$X = \frac{40 - 2S_x}{2}$$
 $Y = \frac{65 - 2S_y}{2}$

4. In the event it is not possible to centralize the impact point and the impact point is located A miles east of the western boundary and B miles north of the WSNM, then use the following formula to obtain box limits.

$$X = A - 2S_{x} \qquad Y = B - 2S_{x}$$

- 5. If extended range land is utilized for the rocket firing, then the eastwest box limits may be extended some 2-4 miles.
- * That is the time the final launcher setting angles were determined.

Theoretically this should insure a 95% probability of impact on the missile range (recall the properties of the standard error of estimate are similar to those of the standard deviation). An Aerojet Corporation report would give a lower probability (86-87%) (see Reference 4) where if the inrange standard deviation of the impact point is 6, and the crossrange standard deviation is 6, the probability (p) of impacting within an ellipse with an inrange semi-axis of K6, and a crossrange semi-axis of K6, is:

$$p = 1 - k^2/2$$

Although some of the dispersion statistics may suggest rather large box limits, practical experience has shown that it is probably not a good policy to let box limits exceed ± 15 on the north-south and ± 10 on the east-west.*

It can be readily seen from the formulae that calculate the box limits, that since A 40 and B 65 that to utilize maximum box limits (that is take advantage of the two standard error or estimate lengths), the impact point should be centralized in the range as much as possible.

The standard error of estimate for rocket impact points in component form is given by the following formula:

$$S_{y} = \frac{\sum_{i}^{m} (y_{i} - y_{i})^{2}}{\sum_{i}^{m} (x_{i} - x_{i})^{2}}$$

$$S_{x} = \frac{\sum_{i}^{m} (x_{i} - x_{i})^{2}}{\sum_{i}^{m} (x_{i} - x_{i})^{2}}$$

where $S_{\mathbf{v}}$ is the standard error estimate for the y(N/s) miss component.

 $\mathbf{S}_{\mathbf{v}}$ is the standard error estimate for the $\mathbf{x}(\mathbf{e}/\mathbf{w})$ miss component.

Y is the actual north-south impact.

X is the actual east-west impact.

Y is the predicted north-south impact.

 X_{p} is the predicted east-west impact.

n is the number of cases.

The standard error of estimate has properties analogous to the standard deviation (3); namely, for a large sample, one standard error of estimate comprises 68% of the sample; two standard deviations, like two standard error of estimates, have 95% of the sample and so on.

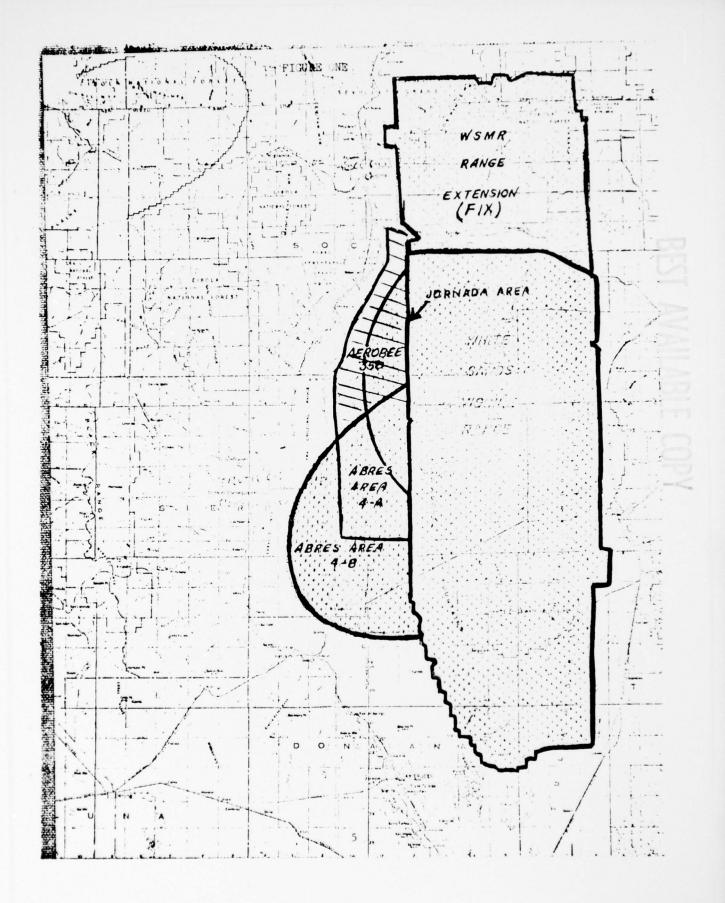
^{*} Based on the premise that the larger the allowable box limits, the larger the permitted wind variability will be; thus, the larger the uncertainty introduced into the impact prediction will be.

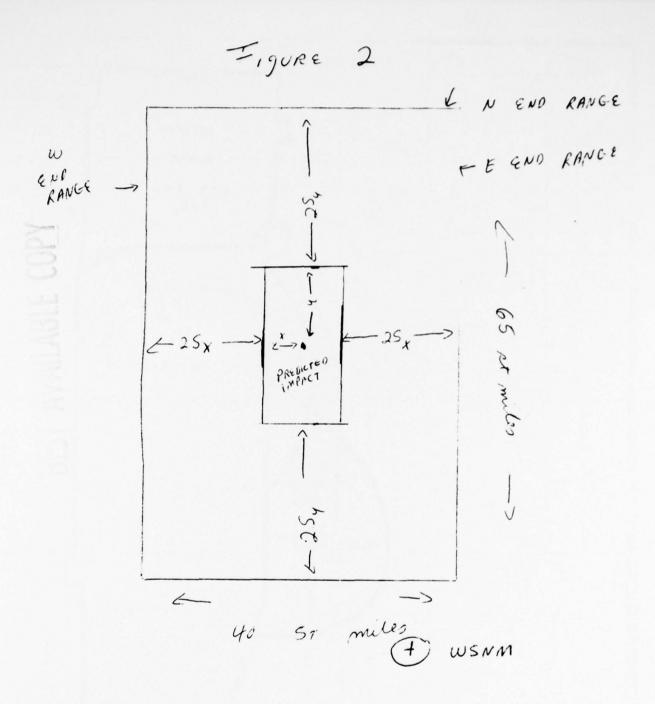
For small samples, $\mathbf{S}_{\mathbf{y}}$ and $\mathbf{S}_{\mathbf{x}}$ should be replaced by

$$S_{y} = \frac{m}{m-2} \qquad S_{x} = \frac{m}{m-2}$$

$$\frac{S}{x} = \frac{m}{m-2}$$

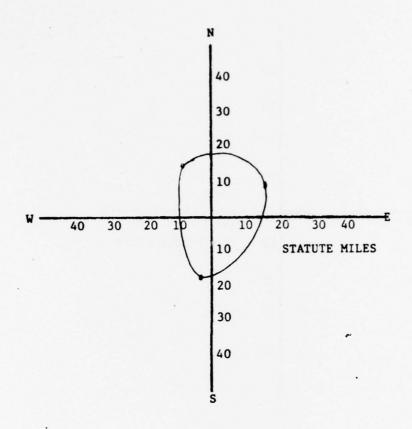
respectively. This modification is likewise analogous to the standard deviation. The standard error of estimate of the total rocket miss is $(S_x + S_y)^{1/2}$.





ROCKET TYPE: BLACK BRANT NUMBER OF CASES: 27

1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W
10.7 8.0 7.0
RECOMME LIED BOX LIMITS

THE ORIGIN IS THE PREDICTED IMPACT.

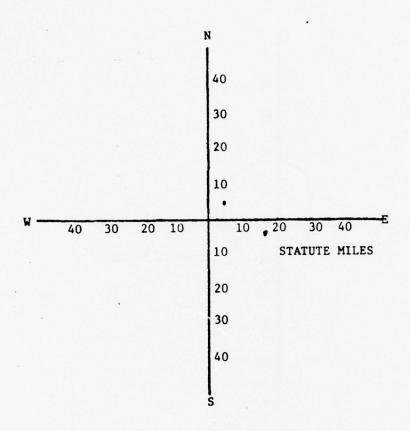
REGUL IR RANGE

+-15 NS +- 6 EW

ROCKET TYPE: NIKE BLACK BRANT

NUMBER OF CASES: 2

1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

 TOTAL
 N/S
 E/W

 9.5
 .4
 9.5

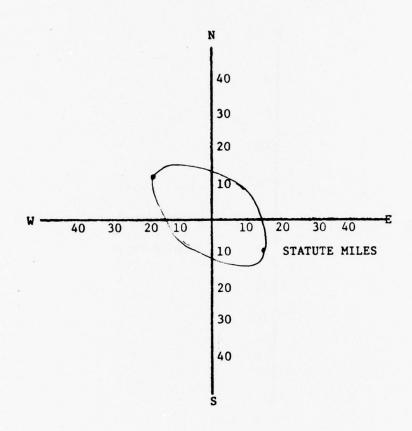
RECOMME IDED BOX LIMITS

REGULAR RANGE EXTENDED RANGE RECOMMENDED

ROCKET TYPE: ATHENA
NUMBER OF CASES: 21

1970-1976

GREEN RIVER UTAH TO MSMR



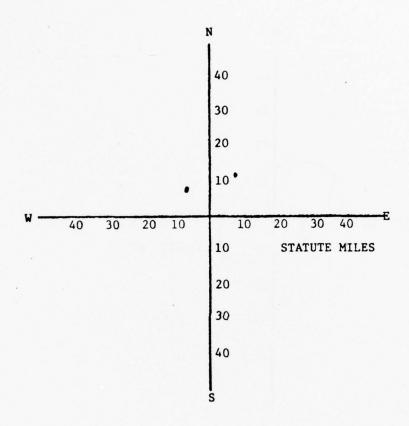
STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL	N/S	E/W
13.8	7.1	11.8

RECOMME LIDED BOX LIMITS
REGULAR RANGE +-9 NS +-6 EW

ROCKET TYPE: NUMBER OF CASES: 1979-1976

PIUTE TOMAHAWK



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W

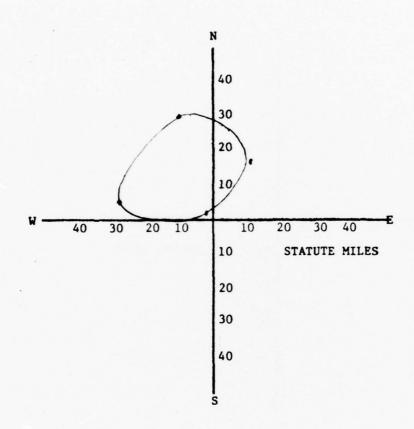
12.7 9.6 8.3

RECOMME DED BOX LIMITS

REGULAR RANGE +-13 NS +-3 EW

ROCKET TYPE: NUMBER OF CASES: 4 1070-1976

UTE TOMAHAMK



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W 24.2 17.6 16.6

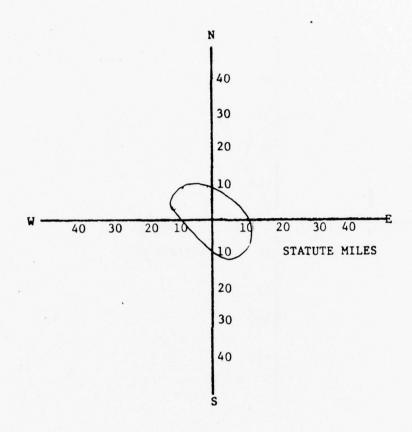
RECOMME LOED BOX LIMITS REGULAR RANGE

RECOMMEND EXTENDED LAND

ROCKET TYPE: NIKE CAJUN

NUMBER OF CASES: 15

1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL 7.7

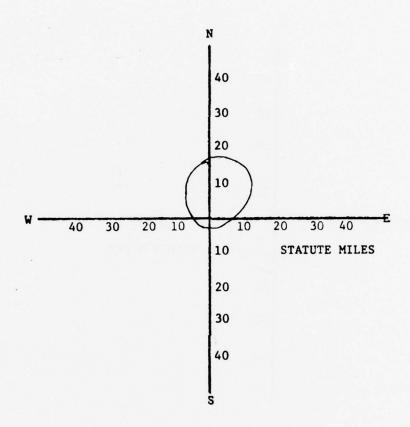
N/S 5.1 E/W 5.8

RECOMME IDED BOX LIMITS REGULAR RANGE

+- 15 NS +-8 EW

ROCKET TYPE: NUMBER OF CASES: 1970-1976

NIKE HYDAC



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

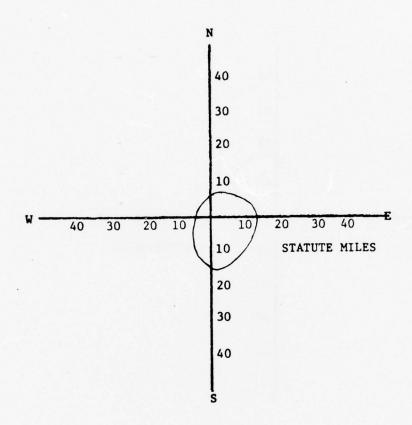
TOTAL N/S E/W 5.4 5.4 6.4

RECOMME LOED BOX LIMITS
REGULAR RANGE +- 15 NS +-7 EW

ROCKET TYPE: NUMBER OF CASES: 6

NIKE IRQUOIS

1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL

N/S

E/W

8.7

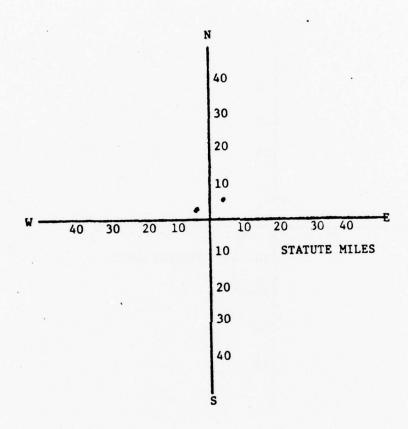
6.7

5.5

RECOMME IDED BOX LIMITS REGUL IR RANGE

+-15 NS +- 9 EW

NUMBER OF CASES: 2



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

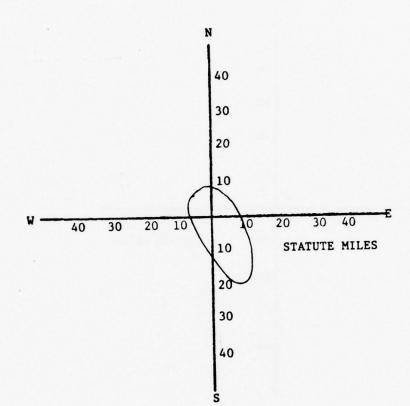
E/W N/S TOTAL

6.7 5.5 3.9

RECOMME LIED BOX LIMITS REGULIR RANGE +-15 NS +- 10 EW

ROCKET TYPE: NIKE APACHE NUMBER OF CASES: 11

1979-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

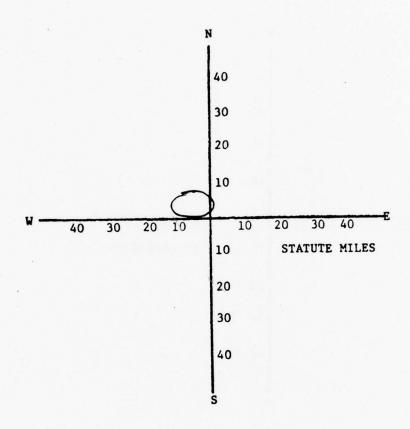
E/W TOTAL N/S 7.8 4.3 8.9

RECOMME LIED BOX LIMITS REGULIR RANGE +- 15 NS +- 10 EW

ROCKET TYPE: NUMBER OF CASES: 4

NIKE TOMAHAWK

1079-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL

N/S

E/W

10.6

6.2

8.6

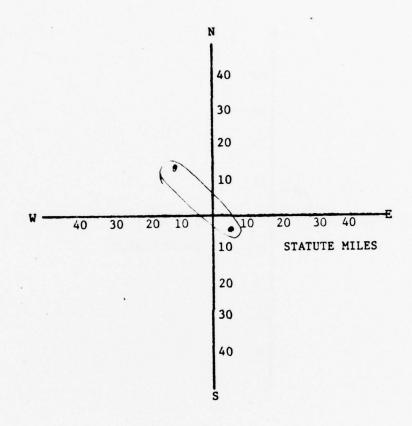
RECOMME LOED BOX LIMITS

REGULAR RANGE

+- 15 N5 +-3 EW

ROCKET TYPE: 1970-1976

HARSES NUMBER OF CASES: 5

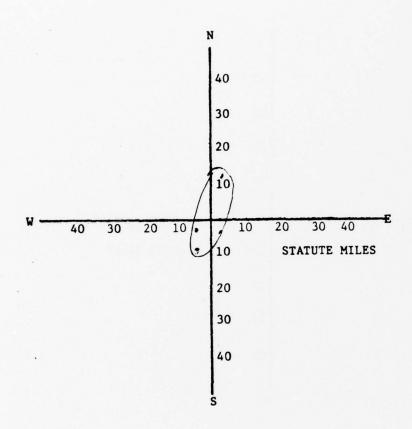


STANDARD ERROR OF ESTIMATE (STATUTE MILES)

N/S E/W TOTAL 12.5 7.6 9.9

RECOMME IDED BOX LIMITS REGULAR RANGE EXTENDED LAND RECOMMENDED

ROCKET TYPE: ASTROBLE D
NUMBER OF CASES: 14



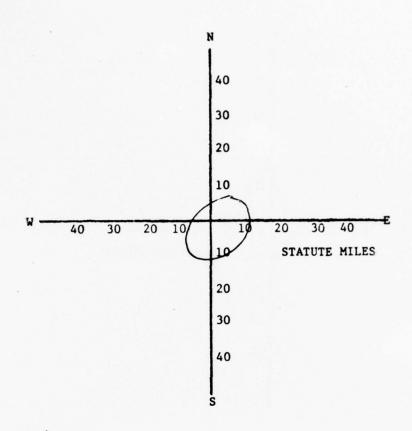
STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W

8.3 6.9 4.6

RECOMME IDED BOX LIMITS
REGULAR RANGE +- 15 NS +- 10 EW

ROCKET TYPE: ASTROBEE F
NUMBER OF CASES: 5
1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

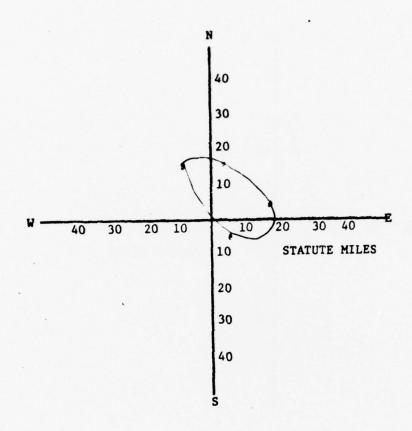
TOTAL N/S E/W
12.6 11.2 6.2

RECOMME LIDED BOX LIMITS
REGULAR RANGE +-10 NS +-7 EW

ROCKET TYPE: NUMBER OF CASES:

AEROBEE 350

1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

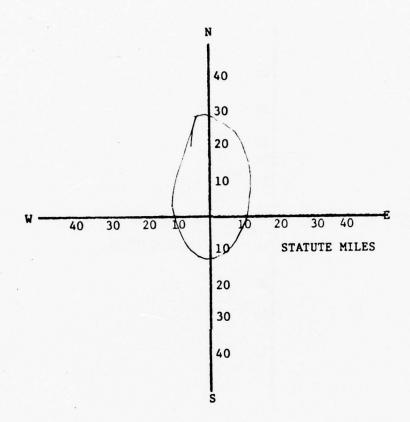
TOTAL N/S E/W
19.0 15.4 11.2

RECOMME LIDED BOX LIMITS REGULAR RANGE

RECOMMED EXTENDED LAND

ROCKET TYPE: AEROBEE 200A

NUMBER OF CASES: 34 1970-1976



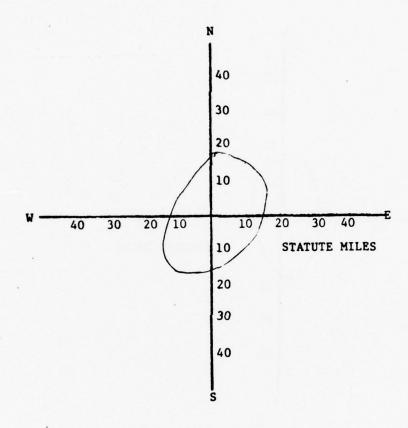
STANDARD ERROR OF ESTIMATE (STATUTE MILES)

N/S E/W TOTAL 8.6 11.9 6.9

RECOMME LOED BOX LIMITS REGULAR RANGE

+- 15 NS +-6 EW

ROCKET TYPE: AEROBEE 200 NUMBER OF CASES: 8

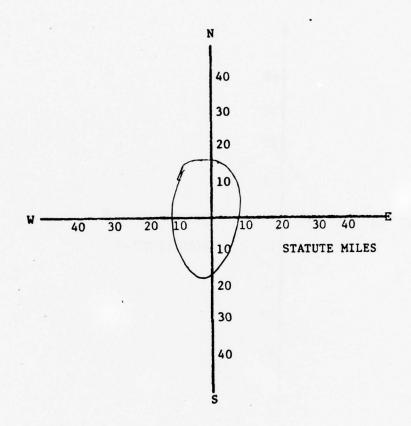


STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W 18.5 13.6 12.5

RECOMME IDED BOX LIMITS
REGULAR RANGE RECOMMED EXTENDED LAND

ROCKET TYPE: ROCKET TYPE: AEROBEE 150
NUMBER OF CASES: 44 1970-1976

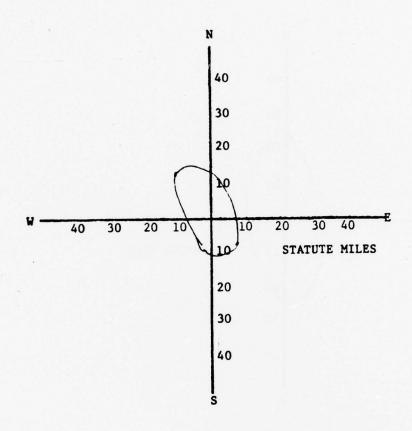


STANDARD ERROR OF ESTIMATE (STATUTE MILES)

N/S E/W TOTAL 9.9 8.3 5.3

RECOMME IDED BOX LIMITS REGUL IR RANGE +-15 NS +- 9 EW

ROCKET TYPE: AMROBEE 170A
NUMBER OF CASES: 22
1979-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

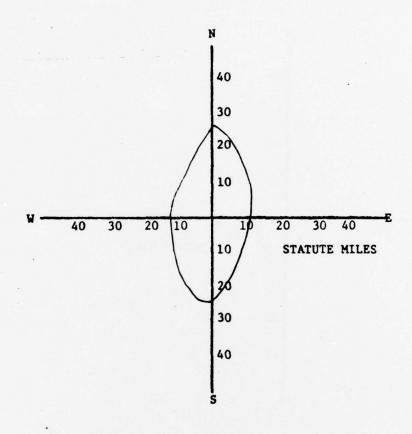
TOTAL N/S E/W 7.8 5.9 5.1

RECOMME LIDED BOX LIMITS
REGULAR RANGE +-15 NS +-9 EW

ROCKET TYPE:

AEROBEE 170

NUMBER OF CASES: 67 1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL

N/S

E/W

13.9

11.8

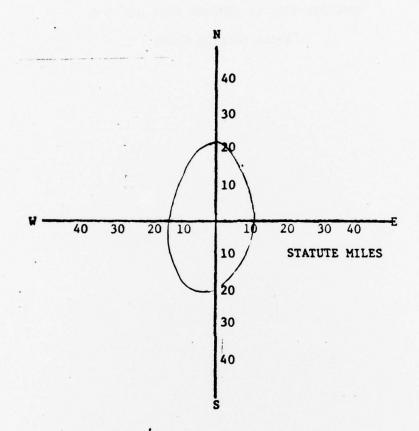
7.4

RECOMME LIED BOX LIMITS REGULIR RANGE

+- 9NS +-5 EW

UNGUIDED MISSILE FIRINGS FROM THE WSMR SMALL MISSILE RANGE

ROCKET TYPE: VIPER LOKI NUMBER OF CASES: 31 1970-1976

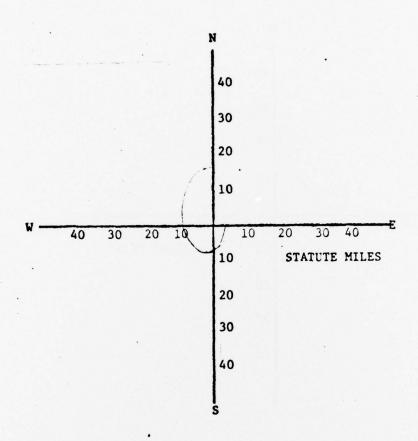


STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W 10.4 8.9 5.3

RECOME LOED BOX LIMITS plus/minus 5 N/S plus/minus 5 E/W

ROCKET TYPE: LOKI NUMBER OF CASES: 144 1070-1976 (1975-1976 sample)



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

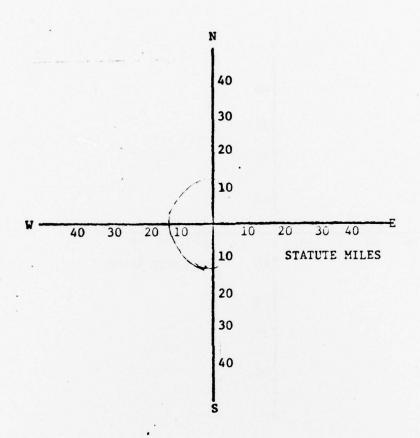
TOTAL N/S E/W 5.73 4.1 4.0

RECOME LIED BOX LIMITS
REGULAR RANGE

plus/minus 7 N/S plus/minus 7 E/W

ROCKET TYPE: SUPER LOKI NUMBER OF CASES: 149

1970-1976



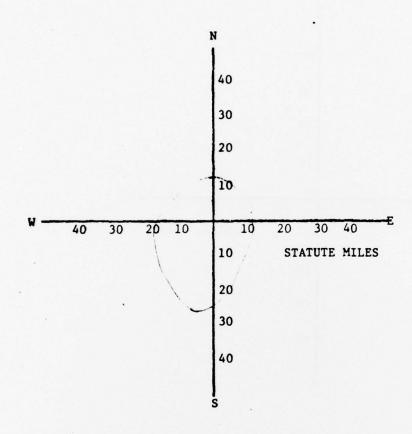
STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S 5.7

E/W 3.6

RECOMME LOED BOX LIMITS
REGULAR RANGE plus/minus 4 N/S plus/Minus 7 E/W

ROCKET TYPE: RDTE
NUMBER OF CASES: 89

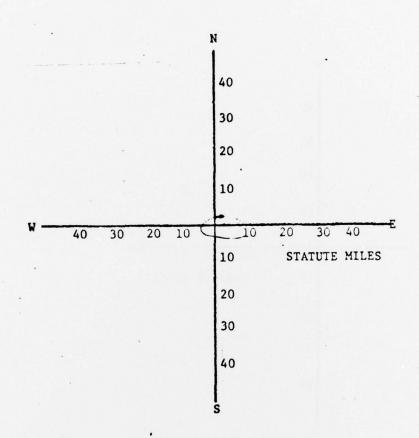


STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W 11.2 8.5 7.3

RECOMME LOED BOX LIMITS
RECULAR RANGE plus/minus 3 N/S and E/W

ROCKET TYPE: MDSS NUMBER OF CASES: 5 1979-1976

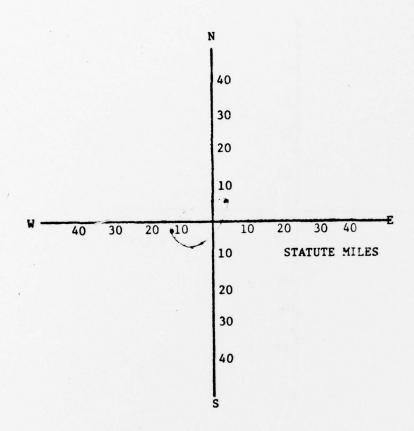


STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W 5.0

RECOME LIED BOX LIMITS
REGULIR RANGE plus/minus 13 N/S plus/minus 5, E/W

ROCKET TYPE: QUANNAH NUMBER OF CASES: 12 1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

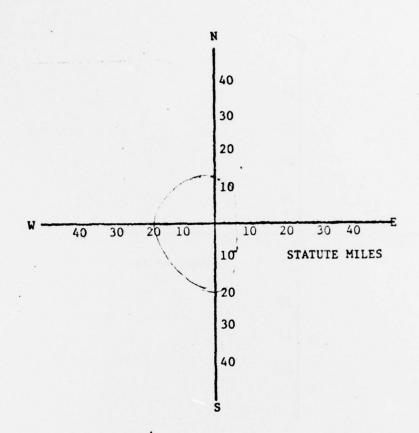
TOTAL N/S E/W 8.2 4.5 6.8

RECOME LED BOX LIMITS

REGULIR RANGE plus/minus 5 N/8 plus/minus 4 E/W

ROCKET TYPE: NUMBER OF CASES: 1970-1976

ARCAS (GAS GENERATED) 183



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

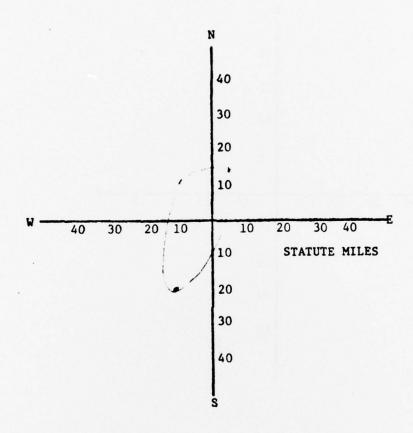
N/S E/W TOTAL 6.9 9.0 5.8

RECOMM DED BOX LIMITS REGUL IR RANGE

plus/minus 3 N/S plus/minus 5 E/W

ROCKET TYPE: SUPER ARCAS NUMBER OF CASES: 6

1070-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

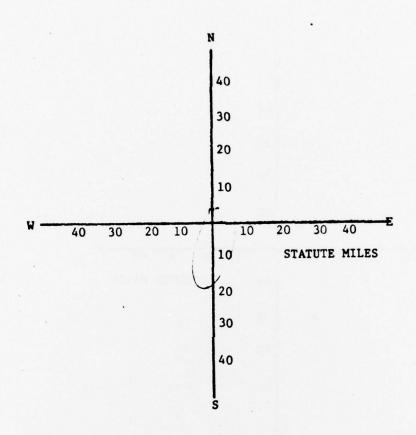
N/S TOTAL E/W 15.6 13.6 7.7

RECOMME LIED BOX LIMITS REGULIR RANGE

plus/minus 10 N/S plus/minus 3 E/W

ROCKET TYPE: HVAR BOCSTED ARCAS NUMBER OF CASES: 4

1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

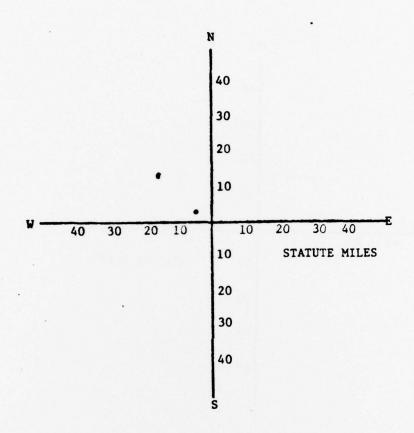
N/S E/W TOTAL 10.4 3.7 11.0

RECOMME LIED BOX LIMITS REGULAR RANGE

plus/minus 5 N/S plus/minus 8 E/W

ROCKET TYPE: SPARROW ARCAS NUMBER OF CASES: 2

1079-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

N/S E/W TOTAL 15.6 8.9 12.7

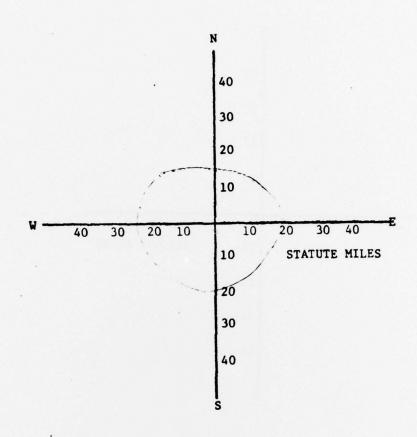
RECOMME LIED BOX LIMITS RECUL IR RANGE

RECOMMEND EXTENDED RANGE

ROCKET TYPE: BOOSTED SIDEWINDER ARCAS

NUMBER OF CASES: 24

1970-1976



STANDARD ERROR OF ESTIMATE (STATUTE MILES)

TOTAL N/S E/W 12.5 8.0 9.6

RECOMME IDED BOX LIMITS
REGULIR RANGE

RECOMMEND EXTENDED RANGE

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- 4. Aerojet-General Corporation (Space General), "Rail Launch Dispersion and Wind Weighting Analysis," Report No. SG 1316TR-5/March 1970.
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